Bush 631-603: Quantitative Methods Lecture 12 (04.11.2023): Uncertainty vol. II

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What is today's plan?

- Calculating uncertainty: beyond measures of spread.
- Hypotheses tests
- When our results are 'significant'?
- Errors in testing.
- How to create efficient visual presentations?
- Power analysis.
- R work: pnorm(),t.test(),power.prop.test(),power.t.test()

Final project

Your research proposals, few lessons:

- Clear description of topic.
- Literature: used to build your arguments.
- Define concepts and main issues.
- ► No tech terms like correlation in introduction.

Our data - our research interests

Making inferences from data to population



Uncertainty

- Our proposed results:
 - Regime type matters for the extent of aid provision.
 - ▶ Financial incentives increase support for anti-plastic campaign.
- Are these effects real or just noise?

Estimation

- Quantity of interest in population.
- Point estimation \rightarrow a 'best guess'.

 $\hat{ heta} = ar{X_n} o$ population p

- CLT and large samples \rightarrow sample proportion = population.
- Experiments: diff-iin-means estimator.
- ATE in population.

Uncertainty tools

More ways to quantify uncertainty:

- SD: variation of estimator ('spread' of distribution).
- Only relevant for simulation.
- Use SE for single sample.

- Confidence intervals:
 - Range of estimator true values.
 - The interpretation of Cls.

Simulate Cls

How many overlap with 'true' support?



Testing our findings

Describing uncertainty of results:

- ► SD/SE.
- Confidence intervals.
- Direct testing of results:
 - Hypothesis testing.
 - Significant effects.

The tea tasting experiment

The scenarios:

Cups	Lady's guess	Actual order	Scenarios			
1	М	М	Т	Т	Т	
2	Т	Т	Т	Т	М	
3	Т	Т	Т	Т	М	
4	М	М	Т	М	М	
5	М	М	М	М	Т	
6	Т	Т	М	М	Т	
7	Т	Т	М	Т	М	
8	М	М	М	М	Т	
Number of correct guesses		8	4	6	2	

Guessing?

- Only one way to choose all 4 cups correctly.
- But 70 ways to choose 4 among 8: $_{8}P_{4} = \frac{8!}{4! + (8-4)!}$
- Assume random choice: equal probability to each combination.
- Chances for guessing all 4 correctly: $\frac{1}{70} = 0.014 = 1.4\%$.

Does not seem like a guess...

Probabilities and guesses



Sampling distribution of Tea Tasting

Simulating tea tasting

What are the odds of n correct cups?

```
# Simulations
sims <- 1000
guess <- c("M","T","T","M","M","T","T","M")</pre>
correct <- rep(NA, sims)</pre>
for (i in 1:sims){
  cups <- sample(c(rep("T",4), rep("M",4)), replace = FALSE)</pre>
  correct[i] <- sum(guess == cups)</pre>
3
head(correct)
## [1] 4 4 6 6 4 4
prop.table(table(correct))
## correct
##
       0
             2 4
                          6
                                 8
## 0.018 0.229 0.536 0.201 0.016
```

Statistical hypothesis testing

A thought experiment - meaningful or random chance?

- Example:
 - You work in a research firm, study social equity.
 - Senior analyst claims 20% of Houston households are poor.
 - Data collection, sample of 950 households in Houston.
 - Mean in sample: 23% under poverty line.

Was the senior analyst wrong? How certain are we that the sample is correct?

Statistical hypothesis testing

- Probabilistic proof by contradiction
- Assume the contrast to our expectations is not possible.



Proof by contradiction

- Houston research firm example
- Assume \rightarrow difference b-w sample and analyst = zero.
- Incorrect? \rightarrow differences exist.
- Senior analyst may have been wrong.
- ▶ We can never **fully** reject a hypothesis (no 100% certainty).

Procedure for hypothesis tests

- (1) Generate a null hypothesis (H_0) .
- A statement we want to refute:
 - A devil's advocate position.
 - Red teams in strategic thinking/wargaming.
- (2) Define alternative hypothesis H_1/H_a .
- Statement of what we actually hope is true.
- Alternative hypothesis is *opposite* of null.
- (3) Show that differences are not due to chance.

Illustrating hypothesis testing

2016 elections polls

Trump consistently outperformed polls in key states

🛑 Trump 💦 🔵 Clinton							
	POLL AVERAGE	POPULAR VOTE COUNT	DIFFERENCE				
National polls	+3	Even	+3				
Missouri	+9	+19	+10				
Wisconsin	+6	+1	+7				
Ohio	+2	+9	+7				
Iowa	+3	+10	+7				
Maine	+9	+3 🚥	+6				
Minnesota	+6	+1	+5				
Michigan	+3	+1 🔳	+4				
North Carolina	Even	+4	+4				
Pennsylvania	+2 🔳	+1	+3 💵				
New Hampshire	+2	Even	+2 💶				
Colorado	+4	+2 💴	+2 🔳				
Georgia	+4	+6	+2 💶				
Florida	+1 🔳	+1	+2 🔳				
Arizona	+3	+4	+1 ■				
Virginia	+5	+5	No difference				
Nevada	+1 🔳	+2 💴	+1 🔳				
THE WASHINGTON POST		:	:				

Illustrating hypothesis testing

- Let's check the 2020 Elections.
- ▶ Final polls: Trump support at 44%.
- ► Actual results: Trump support at 47.5%.
- Is 3% a real difference?

Our Q: true population support for Trump (p).

- Null hypothesis \rightarrow H_0 : p = 0.475
- Alt. hypothesis $\rightarrow H_1 : p \neq 0.475$
- Gather data: sample of about 1300 people.
- Mean proportion: $\bar{X} = 0.44$

Testing our null hypothesis

- If null is true, what the data distribution?
- $X_i...X_n = 1$ if support Trump, 0 otherwise.
- $X_i...X_n$ is Bernoulli with p = 0.475
- Check with simulated data: share of votes in each sample.

```
### Trump support simulation
t_vote <- rbinom(n = 1000, size = 1363, prob = 0.475)
t_share <- t_vote / 1363
head(t share)</pre>
```

[1] 0.4996332 0.4651504 0.4776229 0.4761555 0.4827586 0.4695525

Distribution of estimator

Sample mean vs. simulated proportion of Trump support



Testing our null hypothesis

- Define *p-value*.
- Probability that observed data is as extreme as null.
- If Trump null is true...
- How often we get survey with big polling error?
 - ► Smaller *p*-values ~→ stronger evidence against null.
 - Not probability that null is true!
- p-values are two-sided:
 - Error is 3.5% (0.44 0.475 = -0.035).
 - Check both sides of true mean (p = 0.475).

```
# Error (0.035) in both sides of mean (0.475)
mean(t_share < 0.44) + mean(t_share > 0.51)
```

[1] 0.01

Polling error odds

▶ 1% chance of polling error \rightarrow not too likely



Hypothesis testing expanded

- Directional hypothesis
- Null is incorrect from 'one direction' only.
- Define hypotheses:
 - ▶ Null: *H*₀ : *p* = 0.475
 - one-sided alternative: $H_1: p < 0.475$
 - $H_1 \rightarrow$ polls underestimate Trump support
- Define p-value as one-sided:
 - Probability that random sample underestimate Trump support as we see in our sample?
 - Smaller than two-sided p-value (only left side of distribution!)

Error (0.035) is one-sided
mean(t_share < 0.44)</pre>

[1] 0.006

Final step in hypothesis tests

- Reject the null or not?
- Decide on *threshold* for rejection (test level α)
- Decision rule:
 - Reject null if p-value is below α
 - Otherwise retain the null or fail to reject.
- Common thresholds (α values):
 - $p \ge 0.1$: "not statistically significant".
 - ▶ *p* < 0.05: "statistically significant".
 - p < 0.01: "highly significant".</p>

Decision rule

• Threshold \rightarrow arbitrary (not a 'magic cut-off' points).

- p = 0.051 vs. p = 0.049 ??
- Function of data and sampling procedure.

Ronald Fisher. Journal of the Ministry of Agriculture of Great Britain (1926)

If one in twenty does not seem high enough odds, we may, if we prefer it, draw the line at one in fifty (the 2 per cent. point), or one in a hundred (the 1 per cent. point). Personally, the writer prefers to set a low standard of significance at the 5 per cent. point, and ignore entirely all results which fail to reach this level. A scientific fact should be regarded as experimentally established only if a properly designed experiment *rarely fails* to give this level of significance. The very high odds sometimes claimed for experimental results should usually be discounted, for inaccurate methods of estimating error have far more influence than has the particular standard of significance chosen.

Test errors

- p = 0.05 → extreme data only happen in 5% of repeated samples (if null is true).
- $\blacktriangleright \ \rightsquigarrow 5\%$ of time we reject null that is true!
- Types of errors:

	H ₀ True	H_0 False	
Retain H_0	Awesome!	Type II error	
Reject H_0	Type I error	Good stuff!	

Test errors

What does these errors mean?



Error types

Trade-offs between error types:

- What if we never reject the null?
- ► P(type I) = 0.
- Yet \rightarrow P(type II) = 1.
- Rejecting null: yes/no decision.
- p-value \rightarrow refute the null.
- Not a test of quantity of interest.

Statistical! Not scientific significance

Using visual tools

Main objective:

- Simple presentation of information.
- Clear and straight forward.
- "The eye test": Humans favors color/pictures over numbers.
- Suggested guidelines:
 - How should my product look like?
 - Use graphics instead of text (if possible).
 - Show (me) the data: Annotate plots.
 - Start at zero!
 - Easy-to-read labels and captions.

No, no, no, please NO!!!

Allergy Tablets

INDICATIONS: Provides effective, temporary relief of sneezing, watery and itchy eyes, and runny nose due to hay fever and other upper respiratory allergies.

DIRECTIONS: Adults and children 12 years and over—1 tablet every 4 to 6 hours, not to exceed 6 tablets in 24 hours or as directed by a physician. Children 6 to 11 years—one half the adult dose (break tablet in half) every 4 to 6 hours, not to exceed 3 whole tablets in 24 hours. For children under 6 years, consult a physician.

EACH TABLET CONTAINS: Chlorpheniramine Maleate 4 mg. May also contain (may differ from brand): D&C Yellow No. 10, Lactose, Magnesium Stearate, Microcrystalline Cellulose, Pregelatinized Starch.

WARNINGS: May cause excitability especially in children. Do not take this product unless directed by a physician, if you have a breathing problem such as emphysema or chronic bronchitis, or if you have glaucoma or difficulty in urination due to enlargement of the prostate gland. May cause drowsiness; alcohol, sedatives and tranquilizers may increase the drowsiness effect. Avoid alcoholic beverages, and do not take this product if you are taking sedatives or tranquilizers without first consulting your physician. Use caution when driving a motor vehicle or operating machinery. As with any drug, if you are pregnant or nursing a baby, seek the advice of a health professional before using this product. Keep this and all drugs out of the reach of children. In case of accidental overdose, seek professional

assistance or contact a Poison Control Center immediately.

Store at controlled room temperature 2°-30°C (36°-86°F).

Use by expiration date printed on package.

Protect from excessive moisture.

For better identification keep tablets in carton until used.



Made in U.S.A.

Better...

Drug Facts Active ingredient (in each tablet) Chompeniamine maleate 2 mg. Anthistamine						
Uses temporarily relieves these symptoms due to hay fever or other upper respiratory allergies: sneezing runny nose litchy, watery eyes litchy throat						
Warnings Ask a doctor before use if you have ■ glaucoma ■ a breathing problem such as emphysema or chronic bronchitis ■ trouble urinating due to an enlarged prostate gland Ask a doctor or pharmacist before use if you are taking tranquilizers or sedatives When using this product ■ drouble urinating due to an enlarged prostate gland Ask a doctor or pharmacist before use if you are taking tranquilizers or sedatives When using this product ■ drouble, sedatives, and tranquilizers may increase drowsiness ■ be careful when driving a motor vehicle or operating machinery ■ excitability may occur, especially in children If pregnant or breast-feeding, ask a health professional before use. Keep out of reach of children. In case of overdose, get medical help or contact a Poisor. Control Center right away.						
Directions adults and children 12 years and over not more than 12 tablets in 24 hours						
children 6 years to under 12 years take 1 tablet every 4 to 6 hours; not more than 6 tablets in 24 hours						
children under 6 years ask a doctor						

Colors, captions to convey information

US Public Transportation System Energy Consumption (2019)



Proportions with donuts...

Share of Consumption:

Top 8 states



Michigan

New Jersey

New York

Ohio

California

Illinois

Rest

Texas

Penn

US Gas Monthly consumption share: Top 8 states (June 1993; January 2012)

Show the data: annotations...



'Break Free from Plastic' cleaning campaigns (2019-2020)

More info: break/reefromplastic.org or #break/reefromplastic

Visual tools: let's get technical

- The how?
 - Canva.
 - Piktochart.
 - Venngage.
 - Generate PDF.
 - Print at Copy corner (about \$10).
- More resources?
 - Useful tips \rightarrow (VideoLink)
 - Cindy Raisor.

One sample tests

- Our sample mean meaningful or random?
- ► Not just for binary r.v.s (Trump support).
- Steps for testing:
 - 1. Define null and alternative hyps $(H_0; H_1)$.
 - 2. Select *test statistic* and level of test (α).
 - 3. Derive reference distribution of measure under null.
 - 4. Calculate p-values.
 - 5. Make a decision: reject/retain.

One sample tests

Test statistic:

- Function of data.
- Used to assess both hypotheses.
- Most common \rightarrow *z*-*score*
- The z-statistic:

$$Z = rac{\bar{X} - \mu}{\sigma / \sqrt{n}}$$

Or:

$$Z = \frac{observed - null}{SE}$$

How many SEs away from the null guess is the sample mean?

Testing sample means

THERMOMETER SCORES

- Attitudes towards groups/concepts (0 ('cold') 100 ('warm') scale).
- American attitudes to other nations (2017)



Americans attitudes: My Homecoming

- Focus on Israel.
- Score of 58 \rightarrow in survey (Scotto and Reifler 2017).
- Recent surveys (Pew, 2019) \rightarrow mean score of 55.
- Did attitudes shift? How 'real' are our survey results?
- Use hypothesis test!!

Testing public attitudes

The set-up:

- *H*₀ : μ = 55
 *H*₁ : μ ≠ 55
- Calculate the z-stat:

$$Z = \frac{\bar{X} - \mu}{\hat{\sigma} / \sqrt{n}} = \frac{58 - 55}{30 / \sqrt{800}} = 2.82$$

- Observed score is about 3 SEs from the null!!
- How unlikely is it??

Testing public attitudes data

$$Z = \frac{\bar{X} - \mu}{\hat{\sigma} / \sqrt{n}}$$

- Check the distribution of z under null.
- Not binomial, use CLT in large samples.
- X ~ N(μ , σ^2)
- z is normal and follows the standard normal (mean 0, SD 1).

Testing public attitudes data in R

What is the p-value of our test?

```
### Israel thermometer
# Define all values
n <- 800
x_bar <- 58
mu <- 55
sd <- 30
se <- (sd/sqrt(n))
# Calculate z-score (2.82)
z_ISR <- (x_bar - mu)/(sd/sqrt(n))
# What is the p-value?
pnorm(-z_ISR)
```

[1] 0.002338867

Our survey plotted

```
▶ z-score (-2.8) and p-value (0.002)
```

```
# Create standard normal distribution data
p.norm <- data.frame(x = c(-4,4))
ggplot(p.norm, aes(x=x)) + stat_function(fun = dnorm) +
geom_area(stat = "function", fun = dnorm, fill = "#00998a", xlim = c(-4,-2.8)) +
geom_area(stat = "function", fun = dnorm, fill = "#00998a", xlim = c(2.8,4)) +
geom_vlime(xintercept = -2.8, color = "red") +
geom_vlime(xintercept = 2.8, color = "red") + xlab("") + ylab("") +
geom_text(aes(x=-3.5, y=0.05, label = "our \n z-stat")) + theme_bw()</pre>
```



Small samples problem

- z-score is useful for large samples under CLT.
- Small sample \rightarrow uncertainty about \bar{X} distribution.
- Assume X_i is normally distributed (not likely!)
- Find t-statistic instead:

$$T = rac{ar{X}-\mu}{\hat{SE}} pprox t_{n-1}$$

- t-distribution with n-1 degrees of freedom.
- Centered around zero.

Test with t-distribution

t-test vs. z-test:

- $z \rightarrow$ normal distribution (large samples, n > 30).
- t \rightarrow t-distribution (smaller samples, more conservative).
- In t-distribution: larger p-values (less likely to reject null).
- One more testing option: construct Cls
- If $\mu = 55$ is not in Cls \rightarrow reject null!

```
# Construct 95% and 99% CIs for x_bar = 58
c(x_bar - qnorm(0.995) * se, x_bar + qnorm(0.995) * se)
```

```
## [1] 55.26792 60.73208
c(x_bar - qnorm(0.975) * se, x_bar + qnorm(0.975) * se)
```

[1] 55.92114 60.07886

Test for proportions

- Trump support numbers again: survey (0.44); actual (0.475).
- prop.test(): calculate p-value and 95% Cls.

```
# 600 supports in 1363 sample (x-bar)
prop.test(600, n = 1363, p = 0.475, correct = FALSE)
##
## 1-sample proportions test without continuity correction
##
## data: 600 out of 1363, null probability 0.475
## X-squared = 6.6171, df = 1, p-value = 0.0101
## alternative hypothesis: true p is not equal to 0.475
## 95 percent confidence interval:
## 0.4140563 0.4666907
## sample estimates:
## p
## 0.4402054
```

Two sample tests

- Goal: learn about population differnece in means.
- Compare differences b-w multiple groups: same testing procedures.
- Define:
 - Null PATE \rightarrow H_0 : $\mu_T \mu_C = 0$
 - Alt. PATE \rightarrow $H_1: \mu_T \mu_C \neq 0$
 - Test statistic: diff-in-means estimator.
 - z-score for two sample z-test.
- Are the differences in sample means just random chance?

Two sample test: generating data

- Generate experimental data (recipient regime and foreign aid)
- Focus on treatment 1 (regime type) & continuous DV (extent of aid)

head(exp.dat, n=8)

##		ID	trt1	trt2	dv_cor1	dv_cor2	$cont_cor1$	cont_cor2
##	1	0001	1	0	1	0	1523.100	1395.533
##	2	0002	1	1	1	1	1492.402	1466.578
##	3	0003	1	0	1	0	1500.165	1431.904
##	4	0004	1	0	1	0	1510.011	1406.666
##	5	0005	0	1	0	1	1515.649	1442.158
##	6	0006	0	0	0	0	1512.053	1430.640
##	7	0007	0	0	0	1	1474.265	1451.380
##	8	8000	1	1	1	0	1498.759	1443.719

Two sample test

Define groups to compare in the data

```
Run a two sample t-test
```

```
##
## Welch Two Sample t-test
##
## data: exp.dat$cont_cor1[exp.dat$trt1 == 0] and exp.dat$cont_cor1[exp.dat$tr
## t = -13.697, df = 993.53, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -23.59653 -17.68267
## sample estimates:
## mean of x mean of y
## 1489.333 1509.973</pre>
```

Two sample test

The data

Hawk/Dove leader and FP actions (Mattes and Weeks 2019)

head(hawksdata, n=3) ## # A tibble: 3 x 32 ## caseid hawk t party t rappr~1 succe~2 hawk intl trust voted16 polac~3 <dbl> <dbl+l> <db ## ## 1 3.29e8 2 [Dip~ 1 [Rep~ 1 [Red~ 1 [Pul~ 4 [Agr~ 4 [Agr~ 2 [The~ 4 [Yes~ 1 [sel~ ## 2 3.29e8 1 [Mil~ 1 [Rep~ 1 [Red~ 1 [Pul~ 2 [Dis~ 4 [Agr~ 2 [The~ 4 [Yes~ 2 [not~ ## 3 3.29e8 1 [Mil~ 2 [Dem~ 1 [Red~ 1 [Pul~ 2 [Dis~ 2 [Dis~ 2 [The~ 4 [Yes~ 1 [sel~ ## # ... with 22 more variables: polact 2 <dbl+lbl>, polact 3 <dbl+lbl>, polact 4 <dbl+lbl>, hddv1 <dbl+lbl>, hdmed1 strat <dbl+lbl>, ## # ## # hdmed1 pacifist <dbl+lbl>, hdmed1 warmonger <dbl+lbl>, hddv2 <dbl+lbl>, hdmed2_strat <dbl+lbl>, hdmed2_pacifist <dbl+lbl>, ## # ## # hdmed2 warmonger <dbl+lbl>, birthvr <dbl>, gender <dbl+lbl>, educ <dbl+lbl>, pid3 <dbl+lbl>, pid7 <dbl+lbl>, ideo5 <dbl+lbl>, ## # newsint <dbl+lbl>, pew_religimp <dbl+lbl>, approve_b <dbl>, ... ## # # Groups of support by Hawk/Dove treatment

table(hawksdata\$hawk_t,hawksdata\$hddv1)

##						
##		1	2	3	4	5
##	1	59	132	148	187	74
##	2	73	83	83	217	143

Two sample test

- Does type (hawk/dove) makes a difference?
- Use t-test: compare support (1-5 scale) b-w groups

```
# t-Test
t.test(hawksdata$hddv1[hawksdata$hawk t == 1],
      hawksdatahdv1[hawksdata$hawk t == 2])
##
##
   Welch Two Sample t-test
##
## data: hawksdata$hddv1[hawksdata$hawk_t == 1] and hawksdata$hddv1[hawksdata$
## t = -4.3646, df = 1183, p-value = 1.385e-05
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -0.4577038 -0.1738210
## sample estimates:
## mean of x mean of y
## 3,141667 3,457429
```

Testing failures

- ▶ We fail to reject null, but null is still untrue. Why?
- Sample is too small \rightarrow 'inflates' SEs.



Power Analysis:

- Power = 1 P(type II error).
- Type II error: *false negative*.
- Maximize test power!!!
- Calculate smallest sample size to identify differences.
- Like MOE discussion initial step in survey design
- Minimum sample size to reject the null:
 - Surveys: similar proportion b-w groups (candidates).
 - Experiments: reject zero ATE.

Finding the power...

- Define:
 - 1. Hypothetical sample size.
 - 2. Probability of rejecting null (p-value, α).
 - 3. Proportions of sample and 'population'.

Calculate power of test (preferred power > 0.8).

```
# Define parameters and values
n <- 250
p_bar <- 0.47
p <- 0.5
alpha <- 0.05
cr_value <- qnorm(1 - alpha/2)
se_bar <- sqrt(p_bar * (1-p_bar) / n)
se_p <- sqrt(p * (1-p) / n)
# power
pnorm(p - cr_value * se_p, mean = p_bar, sd = se_bar) +
pnorm(p + cr value * se_p, mean = p_bar, sd = se_bar) +
```

[1] 0.1572895

Now for the power analysis

- Find sample size: power.prop.test() function.
- Define: Groups proportions (p₁, p₂); significance level (α)' power of test.

What is minimum group size? (power = 0.9)
power.prop.test(p1 = 0.5, p2 = 0.45, sig.level = 0.05, power = 0.9)

```
##
##
        Two-sample comparison of proportions power calculation
##
                 n = 2094.153
##
                p1 = 0.5
##
                p2 = 0.45
##
         sig.level = 0.05
##
             power = 0.9
##
##
       alternative = two.sided
##
## NOTE: n is number in *each* group
```

Smaller proportions differences

What is minimum group size? (power = 0.9)
power.prop.test(p1 = 0.05, p2 = 0.1, sig.level = 0.05, power = 0.8)

Two-sample comparison of proportions power calculation ## ## n = 434.432## p1 = 0.05## p2 = 0.1sig.level = 0.05## power = 0.8## alternative = two.sided ## ## ## NOTE: n is number in *each* group

Using power.prop.test() to find the test power

Define sample size and groups proprtions
power.prop.test(n = 100, p1 = 0.05, p2 = 0.1, sig.level = 0.05)

Two-sample comparison of proportions power calculation ## ## n = 100## p1 = 0.05## p2 = 0.1sig.level = 0.05## ## power = 0.2674798alternative = two.sided ## ## ## NOTE: n is number in *each* group

- Continuous variables: *t-test* version of power analysis.
- ▶ One sample: define mean (delta) and SD of r.v. in sample.

• Null:
$$H_0: \bar{X} = 0$$

```
# Minimum sample size
power.t.test(delta = 0.3, sd = 1, type = "one.sample", power = 0.9)
```

```
##
        One-sample t test power calculation
##
##
                 n = 118.6865
##
             delta = 0.3
##
##
                sd = 1
         sig.level = 0.05
##
             power = 0.9
##
       alternative = two.sided
##
```

Two sample: define diff-in-means (delta) and SD.

• Null:
$$H_0: \overline{X_T} - \overline{X_C} = 0$$

```
##
##
        Two-sample t test power calculation
##
                 n = 160.443
##
             delta = 0.3
##
                sd = 1
##
##
         sig.level = 0.05
             power = 0.85
##
       alternative = one.sided
##
##
## NOTE: n is number in *each* group
```

- Two sample: define diff-in-means (delta) and SD.
- For small effects \rightarrow more 'demanding' sample

```
##
##
        Two-sample t test power calculation
##
                 n = 15976.9
##
             delta = 0.03
##
                sd = 1
##
##
         sig.level = 0.05
             power = 0.85
##
       alternative = one.sided
##
##
## NOTE: n is number in *each* group
```

Wrapping up Week 12

Summary:

- Testing uncertainty: beyond measures of spread.
- Hypothesis test: Proof by contradiction.
- The Null and Alternative hypotheses.
- p-value, one-sided or two-sided test.
- When to reject the null? (obtain it?)
- Type I & II errors.
- t-test for sample mean or two groups.
- Power analysis.
- Creating visual display of data tips, software and resources.

Data report by 4/15 midnight!!