

# Bush 631-600: Quantitative Methods

Lecture 6 (10.04.2022): Prediction vol. II

Rotem Dvir

The Bush school of Government and Public Policy

Texas A&M University

Fall 2022

# What is today's plan?

- ▶ Predictions: Improved (and more accurate) methods.
- ▶ Identify correlations in data with plots.
- ▶ The linear model: correlations, predictions, fit.
- ▶ Final project prep: Formulate your research question.
- ▶ R work: `scatterplot()`, `lm()`, `cor()`.

# Framing a message with a plot

## How the Ruble's Value Has Changed

20 rubles per U.S. dollar



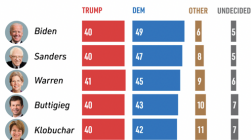
Note: Scale is inverted to show the decline in the ruble's value. Price as of 5:00 p.m. Eastern. Source: FactSet By The New York Times

# Predicting with data

## Elections forecasting

USC Dornsife / Los Angeles Times POLL

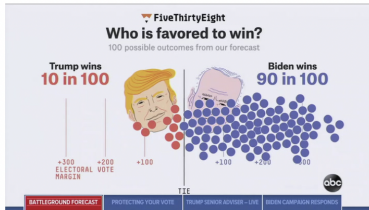
### Trump support tops out at about 4 of 10 voters against field of Democratic candidates



Q. If \_\_\_\_\_ were the Democratic party candidate and Donald Trump were the Republican party candidate, for whom would you be most likely to vote, if the election were held today? (Undecided voters were asked: At this time, would you lean more toward voting for Democratic candidate \_\_\_\_\_ or toward voting for Republican candidate Donald Trump?)

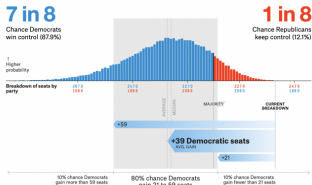
Probability-based internet panel poll conducted January 19 - 26, 2020 by the Understanding America Study at USC Dornsife Center for Economic and Social Research. Participants are members of a panel of more than 6,000 U.S. residents invited to participate in each poll. Margin of sampling error is +/- 2% among U.S. registered voters. The data for Women vs. Trump totals 107 due to rounding. \*Non-fall survey and results at bit.ly/USC20Jan.

Predicting with Polls



### Forecasting the race for the House

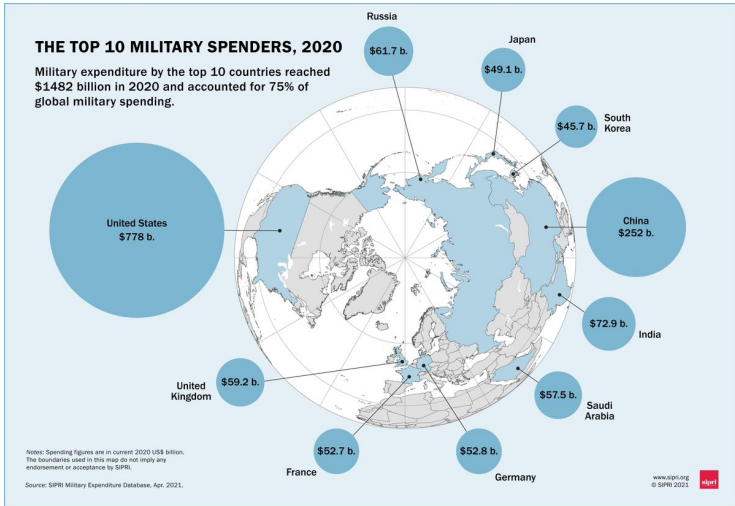
Updated Nov. 8, 2020, at 11:08 AM





# Predicting with data

Military spending → arms race



# Predicting with data

Method:

- ▶ Calculate values per group.
- ▶ Prediction = mean value.
- ▶ Elections: 51 US states (2016).
- ▶ Arms: 157 countries (1999-2019).
- ▶ Main benefit: simple and consistent.
- ▶ Foundation for customer outreach: Purchasing (Amazon); Content (Netflix).

However,

- ▶ Mean → sensitive to outliers/extreme values.
- ▶ Median?
- ▶ 'Ignore' context of special circumstances.

# Better predicting with data

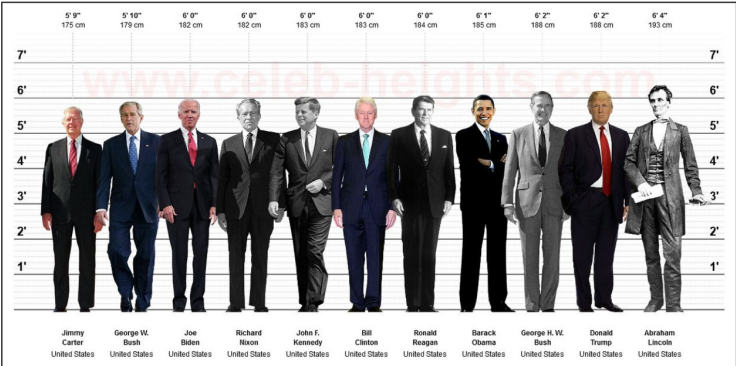
## **Explore linear relationship between factors**

Advanced statistical methods to explore causality:

- ▶ Account for average and extreme values.
- ▶ Account for confounders.
- ▶ Integrate uncertainty in nature.

# Data and linear relationship

## Physical appearance and electoral victory



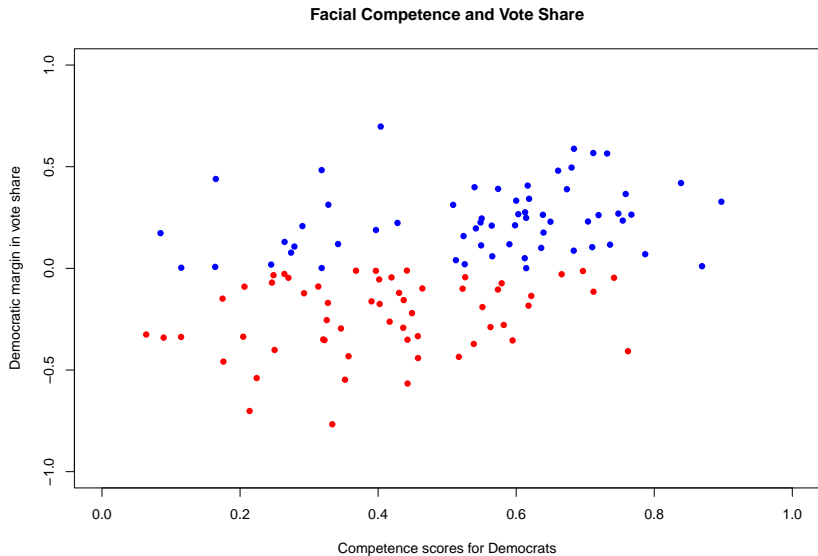
## Data and linear relationship

Facial appearance too?



**Which person is the more competent?**

# Data and linear relationship



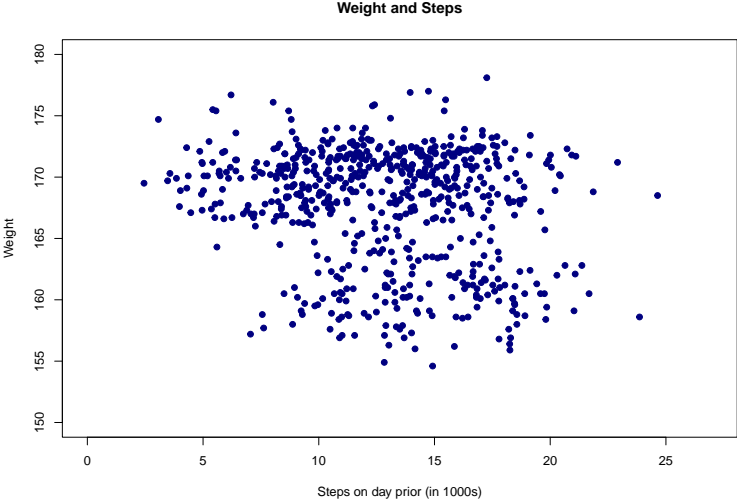
## Checking correlation

- ▶ Upward trend linking competence score and winning.
- ▶ Facial appearance can help winning. . .
- ▶ Is it?

```
# Correlation  
cor(face$d.comp, face$diff.share)
```

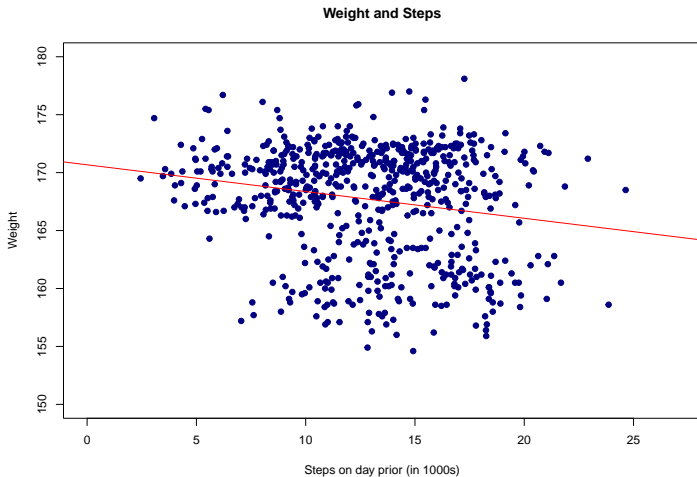
```
## [1] 0.4327743
```

# More examples





# Should I walk to work??



```
cor(health$steps.lag, health$weight)
```

```
## [1] -0.1907032
```

# Identify correlation in data

Correlation and scatter plots:

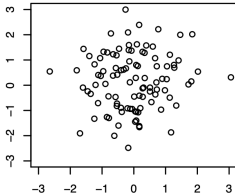
- ▶ Positive correlation → upward slope
- ▶ Negative correlation → downward slope
- ▶ High correlation → tighter, closer to a line
- ▶ Correlation cannot capture nonlinear relationship.

Can we see it?

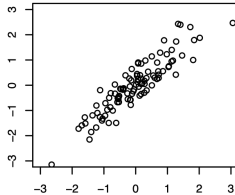
# Identify correlation in data

Scatter plots and correlations:

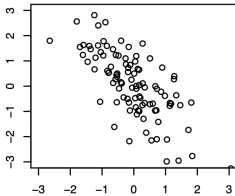
**(a) correlation = 0.08**



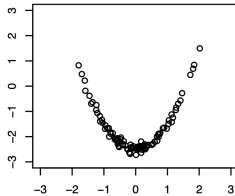
**(b) correlation = 0.91**



**(c) correlation = -0.72**

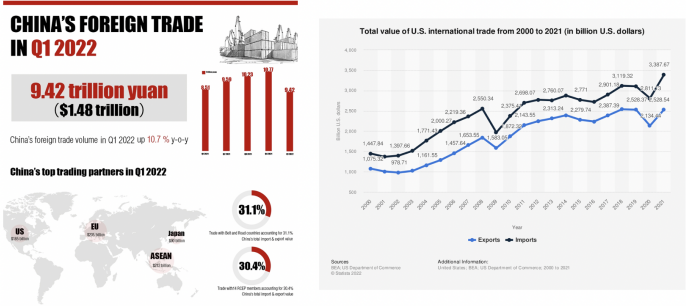


**(d) correlation = 0.12**



# Correlations and predictions: INTA style

## GLOBAL TRADE FLOWS



- ▶ Volume (Q1 - 2022): \$7.7 trillion.
- ▶ Increases in goods and services (20-25% higher than Q1 2021)

# Explaining international trade

## The Gravity Model

- "Workhorse of int'l trade"
- Trade volume b-w countries:
  1. Size of economies.
  2. Distance.



# Measuring Gravity and Trade

- ▶ Distance, land area, population size, borders, etc.

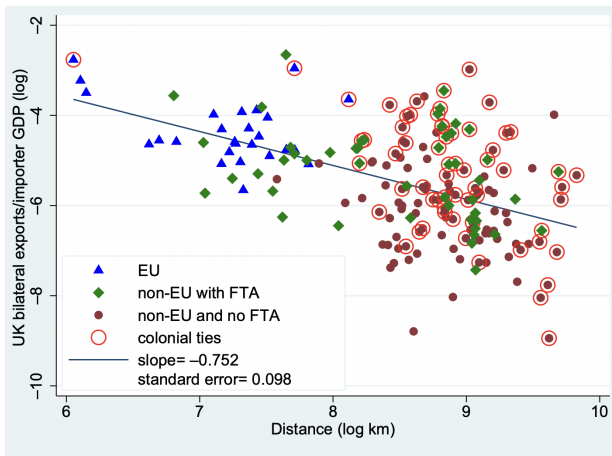


Fig. 2. *UK Bilateral Exports/Importer GDP and Distance, 2017.*

# The Gravity Model

## *Trade and global processes*

- ▶ International conflict / global alliances:
  - ▶ Trade persist b-w strong economies.
  - ▶ Weak and strong economy: trade increases with defense pact.
  - ▶ Weak and strong economy: trade decays with military conflict.
  
- ▶ Move towards Democratization:
  - ▶ Increased trade → consolidate democracy.
  - ▶ Openness (free trade) increase democratization.

# International Trade and democracy promotion

Doces and Magee (2015)

- ▶ Benefits of globalization:
  - ▶ Abundant labor → trade helps workers (and harms capital).
  - ▶ Abundant capital → trade helps capital (and harms workers).
- ▶ Trade → strengthen democracy (labor abundant).
- ▶ Trade → weaken democracy (capital abundant).



# Trade and Democracy

- ▶ Data: democracy and econ (1960-2007)

```
dim(a)
```

```
## [1] 10421    33
```

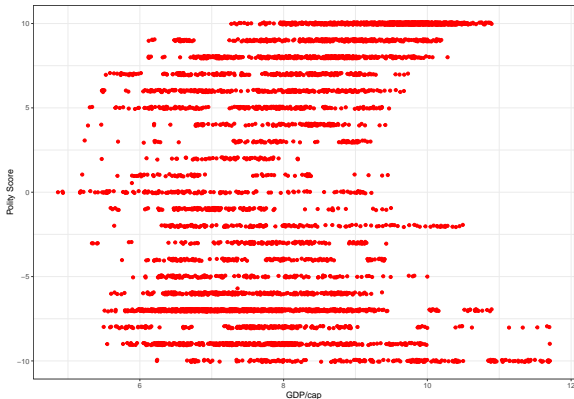
```
head(a, n=5)
```

```
## # A tibble: 5 x 33
```

```
##   year my_code open_hat1 wb_code country pwt_c~1 polity2 America Europe Af
##   <dbl> <dbl> <dbl> <chr> <chr> <dbl> <dbl> <dbl> <dbl> <
## 1 1960      1    15.8 AFG Afghani~ NA -10 0 0
## 2 1961      1    15.7 AFG Afghani~ NA -10 0 0
## 3 1962      1    15.5 AFG Afghani~ NA -10 0 0
## 4 1963      1    16.1 AFG Afghani~ NA -10 0 0
## 5 1964      1    17.5 AFG Afghani~ NA -7 0 0
## # ... with 23 more variables: Pacific <dbl>, oil <dbl>,
## # female_percent_pop <dbl>, pop_15_64 <dbl>, pop_15_under <dbl>, urban <dbl>,
## # region_polity_20 <dbl>, region_polity_10 <dbl>, region_open_20 <dbl>,
## # region_open_10 <dbl>, lang_num2 <dbl>, ethnic_num2 <dbl>,
## # religion_num2 <dbl>, colony_1945 <dbl>, yrs_indep <dbl>, time <dbl>,
## # open3 <dbl>, ln_gdppc8 <dbl>, ln_pop8 <dbl>, kl8 <dbl>, median_kl8 <dbl>,
## # above_median_kl8 <dbl>, above_avg_kl8 <dbl>, and abbreviated variable ..
## # i Use `colnames()` to see all variable names
```

# Gravity model - Trade data

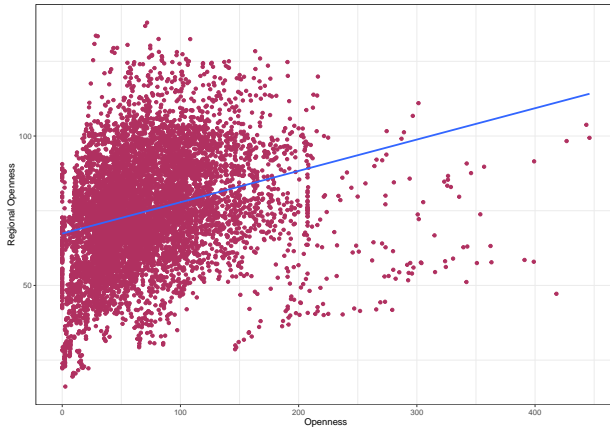
```
ggplot(a, aes(ln_gdppc8, polity2)) +  
  geom_jitter(color = "red") + xlab("GDP/cap") + ylab("Polity Score") +  
  theme_bw()
```



```
cor(a$polity2, a$ln_gdppc8, use = "complete")
```

```
## [1] 0.4396297
```

# Gravity model - Trade data



```
## [1] 0.2756198
```

# Trade and democracy - with a caveat

**Labor abundant** → more workers: Trade boost democracy

```
# Only labor abundant countries  
aa <- a %>%  
  filter(above_median_kl8 == 0)  
  
# Trade and religious diversity  
cor(aa$open3, aa$religion_num2, use = "complete")
```

```
## [1] -0.210249
```

```
# Trade and working population  
cor(aa$open3, aa$pop_15_64, use = "complete")
```

```
## [1] 0.1137331
```

```
# Trade and Democracy  
cor(aa$open_hat1, aa$polity2, use = "complete")
```

```
## [1] 0.1928551
```

# Trade and democracy - with a caveat

**Capital abundant** → less workers: Trade harms democracy

```
# Only capital abundant countries  
aaa <- a %>%  
  filter(above_median_kl8 == 1)  
  
# Trade and religious diversity  
cor(aaa$open3, aaa$religion_num2, use = "complete")
```

```
## [1] 0.3193981
```

```
# Trade and linguistic diversity  
cor(aaa$open3, aaa$lang_num2, use = "complete")
```

```
## [1] 0.2963194
```

```
# Trade and Democracy  
cor(aaa$open_hat1, aaa$polity2, use = "complete")
```

```
## [1] -0.09662274
```

# Least squared

## A LINEAR MODEL

$$Y = \alpha + \beta * X_i + \epsilon$$

Elements of model:

- ▶ *Intercept* ( $\alpha$ ): the average value of Y when X is zero.
- ▶ *Slope* ( $\beta$ ): the average increase in Y when X increases by 1 unit.
- ▶ *Error/disturbance term* ( $\epsilon$ ): the deviation of an observation from a perfect linear relationship.

Our model:

- ▶ **Y** → Democracy score (polity).
- ▶ **X** → Extent of int'l trade (openness).

## Least squared

- ▶ Assumption: model  $\rightsquigarrow$  Data generation process (DGS)
- ▶ **Parameters/coefficients** ( $\alpha, \beta$ ): true values unknown.
- ▶ Use data to estimate  $\alpha, \beta \implies \hat{\alpha}, \hat{\beta}$
- ▶ Predicting (finally!):
  - ▶ Use the *regression line*.
  - ▶ Calculate *fitted value* ( $\neq$  observed value)

$$\hat{Y} = \hat{\alpha} + \hat{\beta} * x$$

## Linear model elements

- ▶ *Residual/prediction error*: the difference b-w fitted and observed values.
- ▶ Real error is unknown  $\Rightarrow \hat{\epsilon}$

$$\hat{\epsilon} = Y - \hat{Y}$$



# Linear model estimation

## Least squared:

- ▶ A method to estimate the regression line.
- ▶ Use data (values of  $Y$  &  $X_i$ ).
- ▶ 'select'  $\hat{\alpha}, \hat{\beta}$  to minimize SSR.
- ▶ Calculate RMSE: average magnitude of prediction error (magnitude of least squared).

$$SSR = \sum_{i=1}^n \hat{\epsilon}^2 = \sum_{i=1}^n (Y_i - \hat{Y}_i)^2 = \sum_{i=1}^n (Y_i - \hat{\alpha} - \hat{\beta} * X_i)^2$$

## Few more points:

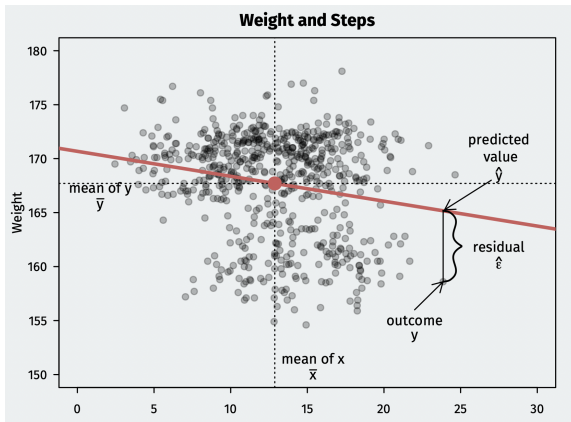
- ▶ Mean of residuals ( $\hat{\epsilon}$ ) == 0.
- ▶ Regression line goes through center of data ( $\bar{X}, \bar{Y}$ ).
- ▶  $\bar{X}, \bar{Y}$ : Sample means of  $X$  &  $Y$ .

# Linear regression in R

## Fit the model

- ▶ Syntax: `lm(Y ~ x, data = mydata)`
- ▶  $Y$  = dependent variable;  $x$  = independent variable(s).

How does it look like?



## Trade and democracy - fitting the model

```
# Fit the model
```

```
fit <- lm(polity2 ~ open3, data = a)  
fit
```

```
##
```

```
## Call:
```

```
## lm(formula = polity2 ~ open3, data = a)
```

```
##
```

```
## Coefficients:
```

```
## (Intercept)          open3
```

```
##    0.711664    -0.006503
```

```
# Directly obtain coefficients
```

```
coef(fit)
```

```
## (Intercept)          open3
```

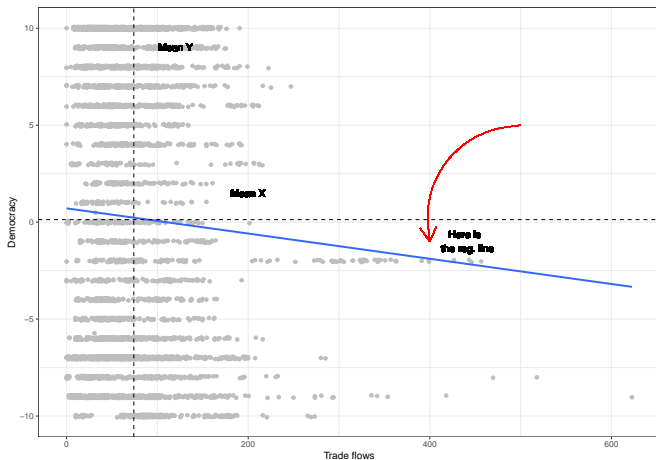
```
## 0.711663968 -0.006502699
```

```
# Directly pull fitted values
```

```
head(fitted(fit))
```

```
##           1           2           3           4           5           6  
## 0.6452021 0.6453733 0.6452360 0.6022816 0.5264752 0.5652951
```

# Trade and democracy - visualize the model



# Trade and democracy - labor vs. capital

```
# Labor abundant
```

```
fit2 <- lm(polity2 ~ open3, data = aa)  
fit2
```

```
##
```

```
## Call:
```

```
## lm(formula = polity2 ~ open3, data = aa)
```

```
##
```

```
## Coefficients:
```

```
## (Intercept)      open3
```

```
##    -3.38618      0.02086
```

```
# Capital abundant
```

```
fit3 <- lm(polity2 ~ open3, data = aaa)  
fit3
```

```
##
```

```
## Call:
```

```
## lm(formula = polity2 ~ open3, data = aaa)
```

```
##
```

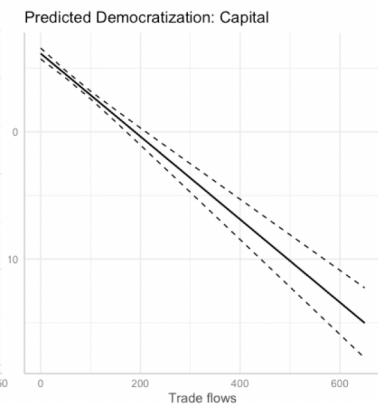
```
## Coefficients:
```

```
## (Intercept)      open3
```

```
##     6.14921    -0.03257
```

# Trade and democracy - labor vs. capital

**Predicted** Polity score  $\leftarrow$  Trade volume



# Least square

- ▶ Regression line  $\rightarrow$  “line of best fit”
- ▶ Minimize prediction error
- ▶ Predictions of fitted line are accurate. How come?
- ▶  $\bar{\hat{\epsilon}} = 0$ .
- ▶ Linear model: not necessarily represent DGS (assumption).

# Errors/Curses/Anomalies



Cursed??





# Errors/Curses/Anomalies



Fighter pilots  
performance?



## How Tall Will Your Child Be?

This formula can be used to predict a healthy range for most children.

**For boys:** Add 5 inches to mother's height, add that number to the father's height and divide by 2.



Source: The Mayo Clinic

**Girls:** Subtract 5 inches from the father's height, add the mother's height and divide by 2.



The Wall Street Journal

My kids height?

# Actually

## REGRESSION TO THE MEAN

- ▶ Empirical - data driven.
- ▶ Explained by (random) chance.
- ▶ High (low) observations are followed by low (high) observations.
- ▶ Observations 'regress' towards the average value of the data.

## Merging data sets

- ▶ Combine data with shared variables.
- ▶ Expand data available: more years, same information.
- ▶ Technical: use columns / rows.
- ▶ Multiple approaches.

# Merging

## (1) merge function:

- ▶ Join two datasets.
- ▶ Merge based on common variable (*by* argument).
- ▶ 2008-2012 voting data: state Abb. name (QSS pp. 150-151).
- ▶ Common variable: matching of rows and columns.
- ▶ Other common columns? Appended with `.x` or `.y` after name.

## (2) cbind function:

- ▶ Column binding of multiple datasets.
- ▶ Main drawback: assumes similar sorting.
- ▶ Keeps duplicates.
- ▶ `rbind()`: join data by rows (add observations to data).

# Merging

## (3) Join (tidyverse):

- ▶ More flexible: multiple options.
- ▶ Keep one data, join by common variable.
- ▶ Keep all data, join by common variable.

			ID	X1				ID	X2																	
			1	a1				2	b1																	
			2	a2				3	b2																	
inner_join			ID	X1	X2	left_join			ID	X1	X2	right_join			ID	X1	X2	full_join			ID	X1	ID	X1		
2	a2	b1	1	a1	NA	2	a2	b1	2	a2	b1	1	a1	NA	2	a2	b1	1	a1	NA	2	a2	1	a1		
			2	a2	b1				3	NA	b2				3	NA	b2									

# Apply prediction with regression

- ▶ Linear model  $\rightarrow$  predict  $Y$  using  $X_i$
- ▶ Using linear predictions - policy:
  - ▶ Predict crime waves - deploy police resources.
  - ▶ Predict students performance - target interventions.
- ▶ Using linear predictions - business:
  - ▶ Predict preferred products based on previous purchases.
  - ▶ Predict Netflix/Spotify content based on what I saw/heard?

# Model fit

Our well does a linear model predict the data (outcome)?

Model fit:

- ▶ Measures to assess model predictive accuracy.

**Coefficient of determination ( $R^2$ ):**

- ▶ The proportion of total variation in outcome explained by model.
- ▶ How much variation in Y explained by our model.
- ▶ Values from 0 (no correlation) to 1 (perfect correlation).

## Model fit: R-squared

$$R^2 = \frac{TSS - SSR}{TSS}$$

TSS (Total sum of squares): prediction error with mean  $Y$  only

$$TSS = \sum_{i=1}^n (Y_i - \bar{Y})^2$$

SSR (Sum of squared residuals): prediction error with model

$$SSR = \sum_{i=1}^n \hat{\epsilon}^2$$



# Model fit with data: Florida (1996-2000)

## Independent candidates 'inertia'?

```
# Use summary function
summary(fit3 <- lm(Buchanan00 ~ Perot96, data = florida))

##
## Call:
## lm(formula = Buchanan00 ~ Perot96, data = florida)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -612.74  -65.96    1.94   32.88  2301.66
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  1.34575    49.75931   0.027   0.979
## Perot96      0.03592     0.00434   8.275 9.47e-12 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 316.4 on 65 degrees of freedom
## Multiple R-squared:  0.513, Adjusted R-squared:  0.5055
## F-statistic: 68.48 on 1 and 65 DF, p-value: 9.474e-12
```

- ▶ 51% of Buchanan (2000) explained by Perot (1996) voters.

## Model fit with data: Florida (1996-2000)

'Conventional' candidates: Clinton - Gore

```
summary(lm(Gore00 ~ Clinton96, data = florida))
```

```
##  
## Call:  
## lm(formula = Gore00 ~ Clinton96, data = florida)  
##  
## Residuals:  
##      Min       1Q   Median       3Q      Max   
## -30689.3 -1161.5  -622.4   1040.3  23309.1   
##  
## Coefficients:  
##              Estimate Std. Error t value Pr(>|t|)      
## (Intercept)  434.49448   921.26520    0.472   0.639      
## Clinton96     1.13120     0.01216   92.997 <2e-16 ***  
## ---  
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1  
##  
## Residual standard error: 6523 on 65 degrees of freedom  
## Multiple R-squared:  0.9925, Adjusted R-squared:  0.9924   
## F-statistic:  8648 on 1 and 65 DF,  p-value: < 2.2e-16
```

# Model fit with data: Florida (1996-2000)

'Conventional' candidates: Dole - Bush

```
summary(lm(Bush00 ~ Dole96, data = florida))
```

```
##  
## Call:  
## lm(formula = Bush00 ~ Dole96, data = florida)  
##  
## Residuals:  
##      Min       1Q   Median       3Q      Max  
## -18276.9  -781.9   -105.3   1599.5  21759.1  
##  
## Coefficients:  
##              Estimate Std. Error t value Pr(>|t|)  
## (Intercept)  799.82813   701.76481     1.14   0.259  
## Dole96        1.27333     0.01262  100.91 <2e-16 ***  
## ---  
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1  
##  
## Residual standard error: 4587 on 65 degrees of freedom  
## Multiple R-squared:  0.9937, Adjusted R-squared:  0.9936  
## F-statistic: 1.018e+04 on 1 and 65 DF,  p-value: < 2.2e-16
```

## Model fit with data: Florida (1996-2000)

Where did the independents go for the millennium?

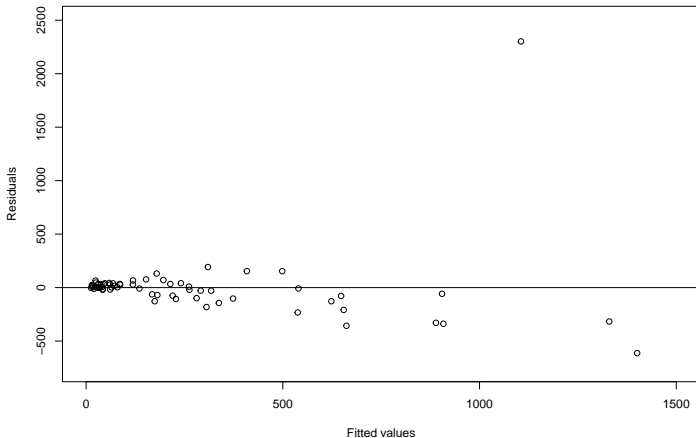
```
summary(lm(Bush00 ~ Perot96, data = florida))
```

```
##  
## Call:  
## lm(formula = Bush00 ~ Perot96, data = florida)  
##  
## Residuals:  
##      Min       1Q   Median       3Q      Max   
## -49100  -5003  -2951   -582 145169   
##  
## Coefficients:  
##              Estimate Std. Error t value Pr(>|t|)      
## (Intercept) 1810.4147  3853.0142   0.47    0.64      
## Perot96      5.7646    0.3361  17.15 <2e-16 ***  
## ---  
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1  
##  
## Residual standard error: 24500 on 65 degrees of freedom  
## Multiple R-squared:  0.8191, Adjusted R-squared:  0.8163   
## F-statistic: 294.2 on 1 and 65 DF,  p-value: < 2.2e-16
```

# Model fit with data: Florida (1996-2000)

Maybe not all of them? *Palm beach county*

```
plot(fitted(fit3), resid(fit3), xlim = c(0,1500), ylim = c(-750,2500),  
     xlab = "Fitted values", ylab = "Residuals")  
abline(h=0)
```



# Model fit with data: Florida (1996-2000)

Remove outlier - better prediction

```
summary(lm(Buchanan00 ~ Perot96, data = florida_cut))
```

```
##
## Call:
## lm(formula = Buchanan00 ~ Perot96, data = florida_cut)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -206.70  -43.51  -16.02   26.92  269.03
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 45.841933  13.892746   3.30  0.00158 **
## Perot96      0.024352   0.001273  19.13 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 87.75 on 64 degrees of freedom
## Multiple R-squared:  0.8512, Adjusted R-squared:  0.8488
## F-statistic:   366 on 1 and 64 DF,  p-value: < 2.2e-16
```

## Model fit

- ▶  $R^2$ : measure of *in-sample* fit.
- ▶ *Out-of-sample-fit*: how model predicts outcomes 'outside' the sample.

### OVERFITTING:

- ▶ OLS → good for in-sample.
- ▶ Poor performance for out-of-sample.
- ▶ Example: use gender to predict 2016 democratic primaries winner.

# Wrapping up week 6

## Summary:

- ▶ Prediction: beyond sample means.
- ▶ Using plots to find correlations/trends in data.
- ▶ Least squared method.
- ▶ Linear model and estimating coefficients.
- ▶ Predictions based on linear model.
- ▶ Merging data.
- ▶ Model fit.



# Looking ahead

- ▶ **Final Project:**
  - ▶ Objective.
  - ▶ Technical aspects.
  
- ▶ Next task - research proposal:
  - ▶ What is the topic / area?
  - ▶ Why important?
  - ▶ How will you study it?
  - ▶ Sources: substance and data.
  - ▶ Final visual product outline.

**Proposal due November 1, 2022**